

Trip to Proxima Centauri calculations

Kinematic Equations:

$$1) v_f^2 - v_0^2 = 2ax$$

$$2) x = 0.5at^2$$

Constants:

$$1) g = 9.8 \text{ m/s}^2 \quad (\text{gravitational acceleration})$$

$$2) c = 3 \times 10^8 \text{ m/s} \quad (\text{speed of light in a vacuum})$$

$$3) D = 4.24 \text{ light years} \quad (\text{Distance from Earth to Proxima Centauri})$$

Calculations:

Distance traveled accelerating at g from rest to 0.92c

$$(0.92c)^2 - (0)^2 = 2gx$$

$$x = (0.92c)^2 \div 2g = (0.92(3 \times 10^8 \text{ m/s}))^2 \div 2(9.8 \text{ m/s}^2) = 3.886530612 \times 10^{15} \text{ m} = \boxed{0.41 \text{ light years}}$$

Time elapsed accelerating at g from rest to 0.92c

$$3.886530612 \times 10^{15} \text{ m} = 0.5gt^2$$

$$t^2 = (3.886530612 \times 10^{15} \text{ m}) \div 0.5(9.8 \text{ m/s}^2)$$

$$t = \text{sqrt}((3.886530612 \times 10^{15} \text{ m}) \div 0.5(9.8 \text{ m/s}^2)) = 28163265.31 \text{ s} = \boxed{0.89 \text{ years}}$$

Distance traveled while coasting at 0.92c

$$x = D - (\text{accelerating distance}) - (\text{decelerating distance}) = D - 0.41 \text{ light years} - 0.41 \text{ light years}$$

$$= 4.24 \text{ light years} - 0.41 \text{ light years} - 0.41 \text{ light years} = \boxed{3.42 \text{ light years}}$$

Time elapsed while coasting at 0.92c

$$t = 3.42 \text{ light years} \div 0.92c = \boxed{3.72 \text{ years}}$$

Total Time Elapsed

$$T = (\text{accelerating time}) + (\text{coasting time}) + (\text{decelerating time})$$

$$= 0.89 \text{ years} + 3.72 \text{ years} + 0.89 \text{ years} = \boxed{5.5 \text{ year}}$$